
2:29 Colliding Steel Balls (D-7)

1. Think about an elastic collision between two steel balls:
 - a. How does the final momentum of the pair compare with the original momentum?

 - b. How does the final kinetic energy of the pair compare with the original KE? _____
2. The target ball is stationary before impact. The projectile ball moves toward the target with velocity " V_0 ". The mass of the projectile is " M ". The target mass differs from the projectile mass by a factor of " R ", so that the target mass is " RM ". (" R " is a *ratio*.) Just after impact the projectile ball has velocity " V_1 " and the target has velocity " V_2 ". Use #1 to see what happens if all three velocities are parallel:
 - a. Show how V_2 can be calculated from V_0 and R . _____
 - b. Show how V_1 can be calculated from V_0 and R . Simplify if possible.

3. The kinetic energy transferred to the second ball is a certain fraction of the original KE.
 - a. Let " A " represent that fraction. Use 2a to show how that "energy transmission efficiency" can be calculated from R . (Remember that the mass of the second ball is RM , not M .) _____
 - b. Let " B " represent the "energy retention efficiency", i.e. the ratio of the energy remaining in the first ball after impact to its original KE. Show how that ratio can be calculated from R . _____
4. Imagine a long series of steel balls suspended as in a "swinging wonder" toy. This set differs from the toy in one important way: These balls do not have equal masses but instead have equal mass *ratios*. The first ball has mass " M " and the last one has mass " ρM ". Let the ratio of any two consecutive masses be " R ", as in #1. Let " $N + 1$ " represent the number of balls in the set. Show how R can be calculated from N and the mass ratio, ρ . Check carefully!

5. Suppose the first ball in the series is given a velocity toward the remaining balls, which hang in a neat, straight row. Show how the KE transmitted to the last ball can be calculated from N , A , and the original KE. _____
6. We want to find the limit of that "overall energy transmission efficiency" as N goes to infinity.
 - a. First, use 3a to eliminate " A " from equation 5. That gives us the overall efficiency in terms of R : _____
 - b. Is the limit obvious in equation 6a? _____

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7. Here's a trick that may be helpful for #6: Notice that when N becomes great, R grows closer and closer to _____. (Give the limiting numerical value of R .)
- a. Therefore we should choose a letter such as " δ " (delta) to represent the *difference* between R and its limiting value. Thus we shall replace R in 6a with _____ - _____.
 - b. For example, if $R = 0.98$ then each mass is _____% less than the previous mass, so $\delta =$ _____.
 - c. The squared binomial in our revised version of eq. 6a then has a big term and a very small term. After squaring it, you have a big term, a small term, and an insignificant term which can be dropped. Then a miracle happens during routine simplification. Try it! Then make a conclusion answering question 6. (Remember that "efficiency" is a *dimensionless ratio*.)

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8. Suppose the first ball in the series is a 5-kg cannonball with a speed of 1 m/s, and the last one is a 30-gram ball bearing. How fast will the ball bearing go just after impact? Explain your answer clearly enough so that *even a physics teacher* can understand it.
